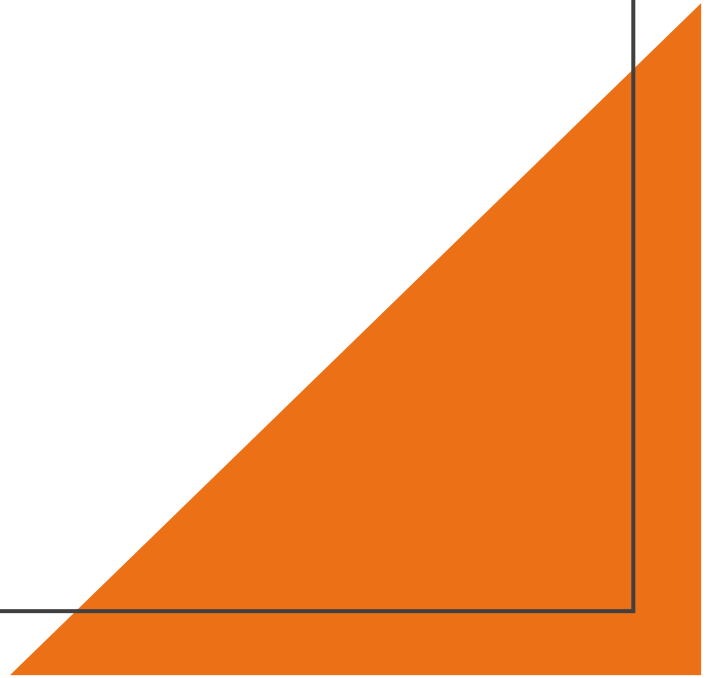


INVENTORY MANAGEMENT ANALYSIS

WHOLESALE FOOD DISTRIBUTOR

OPRE 6304 – Spring 2021

Team 5





Agenda of Items

1. Overview
2. Data Exploration
3. Methodology
4. Findings
5. Recommendations
6. Limitations and Implementation Issues

I. OVERVIEW

GOAL



- Optimize safety stock
- Minimize inventory cost

SCOPE



- Tier 1 has high-priority SKUs
- Tier 2 has low-priority SKUs

REQUIREMENT

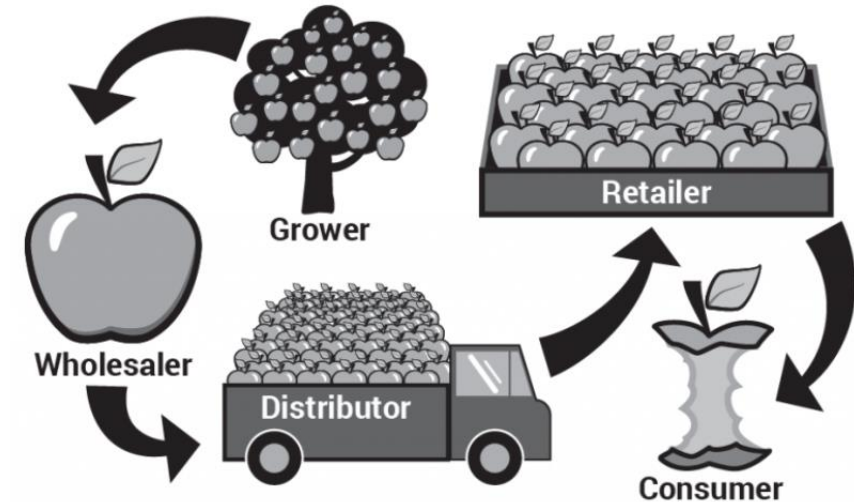


- Maintain 99% service level

I. OVERVIEW

Industry Background – Wholesale Food Distribution

- **Break bulk** and be an intermediary between food producers and food operators
- **Warehouse** products and usually **transport** them to operators
- Distributor purchases, stores, sells, and delivers those products, providing food service operators with access to items from a wide variety of manufacturers.
- Food service distributors need to schedule, track, and manage inventory related to food storage and distribution. They also need to plan shipments, manage customers, and maintain well-documented records of food orders.



II. DATA EXPLORATION

Dataset Information:

- From a wholesale food distributor based out of Chicago area
- Include daily transactions from May - August 2019 with a total of over 45,800 records and 680 unique SKUs
- Have 3 information layers: Transaction, Sourcing and Product



II. DATA EXPLORATION

Transaction

- Delivery Date
- Sum of Quantity (Sales Quantity)
- SKU ID

Sourcing

- SKU ID
- Lead Time
- Minimum Order Quantity (MOQ)

Product

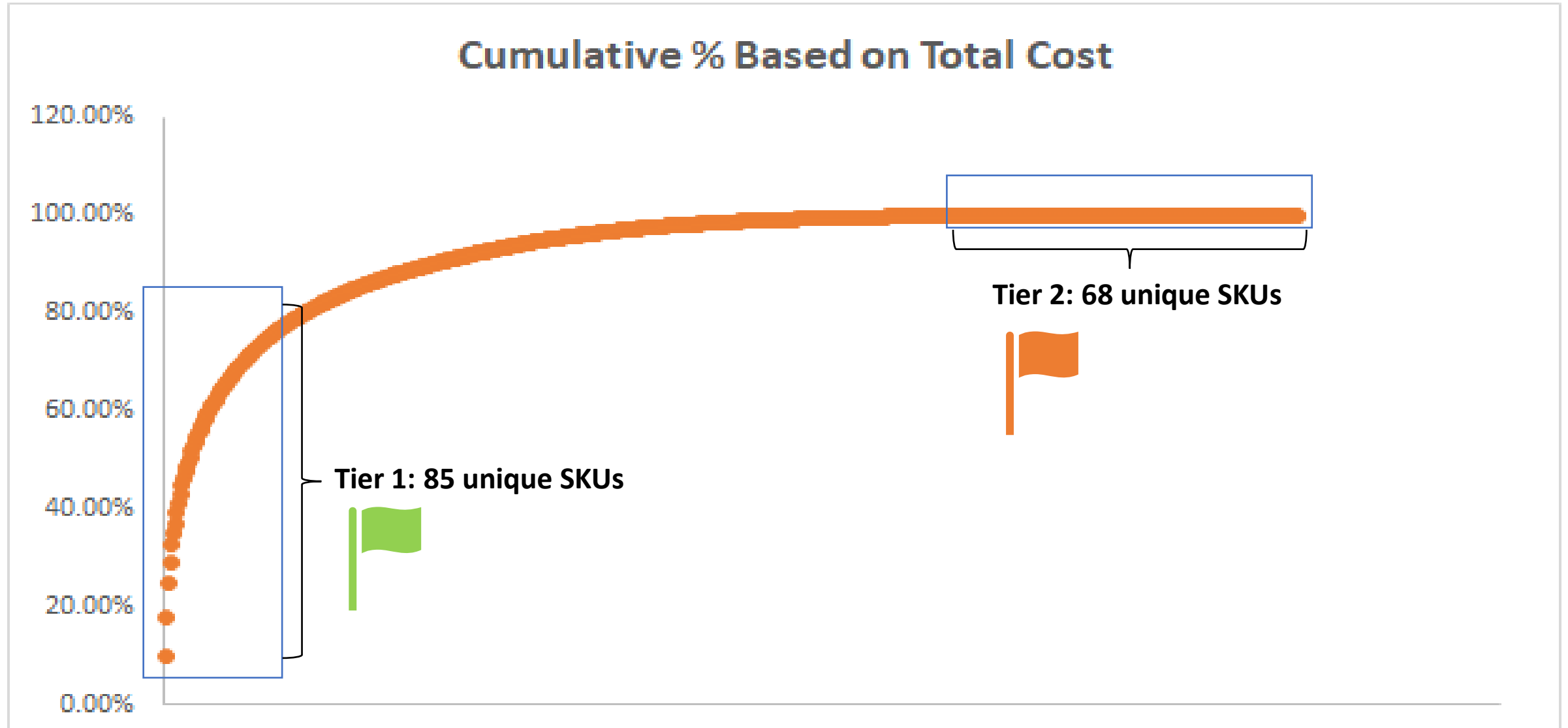
- SKU ID
- Inventory Value
- Continuous Review Policy
- Carrying cost of 10% (Holding Cost)

| Upd_DCName | deliverydate | SUMOfqty | SKU ID |
|------------|--------------|----------|--------|
| DC A | 5/5/2019 | 2 | 186 |
| DC A | 5/5/2019 | 19 | 161 |
| DC A | 5/5/2019 | 32 | 257 |
| DC A | 5/5/2019 | 48 | 499 |
| DC A | 5/5/2019 | 584 | 402 |
| DC A | 5/5/2019 | 5 | 730 |

| Status | Lead Time | MOQ | Production Policy | SKU ID |
|---------|-----------|-----|-------------------|--------|
| Include | 9.25 | 528 | Make | 668 |
| Include | 7.25 | 180 | Make | 716 |
| Include | 9.25 | 42 | Make | 241 |
| Include | 9.25 | 21 | Make | 732 |
| Include | 7.25 | 400 | Make | 683 |
| Include | 9.25 | 18 | Make | 489 |

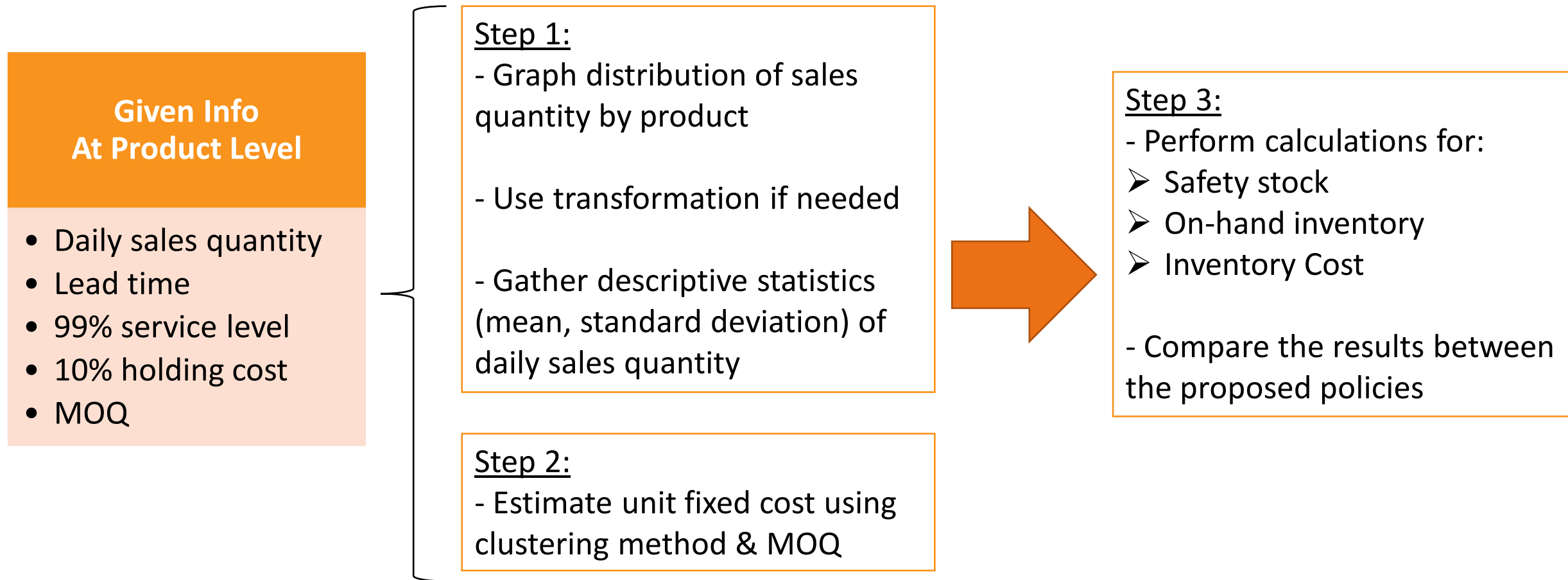
| Upd_DCName | InventoryValue | Review Period | Stocking Site | Status | Carrying Cost | SKU ID |
|------------|----------------|---------------|---------------|---------|---------------|--------|
| DC A | 6.42 | Continuous | TRUE | Include | 10% | 100 |
| DC A | 21.49 | Continuous | TRUE | Include | 10% | 101 |
| DC A | 24.43 | Continuous | TRUE | Include | 10% | 102 |
| DC A | 39.45 | Continuous | TRUE | Include | 10% | 103 |
| DC A | 11.86 | Continuous | TRUE | Include | 10% | 104 |

II. DATA EXPLORATION



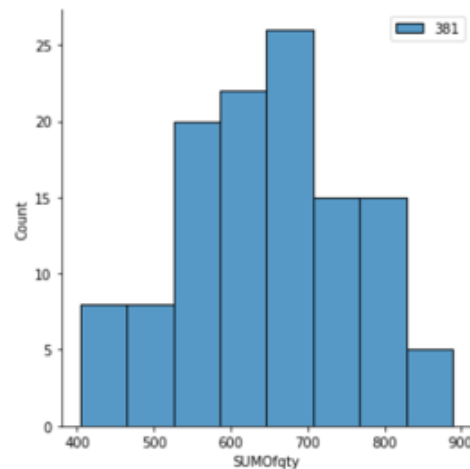
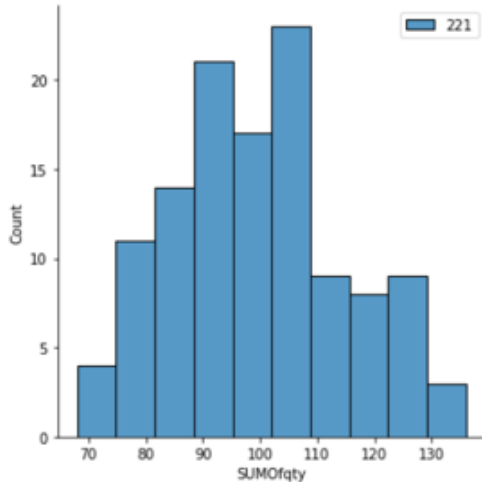
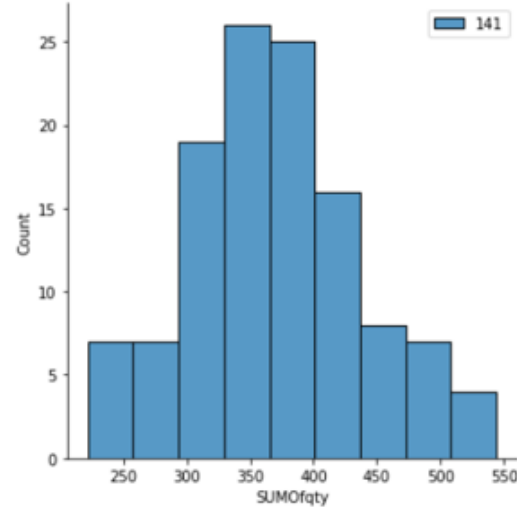
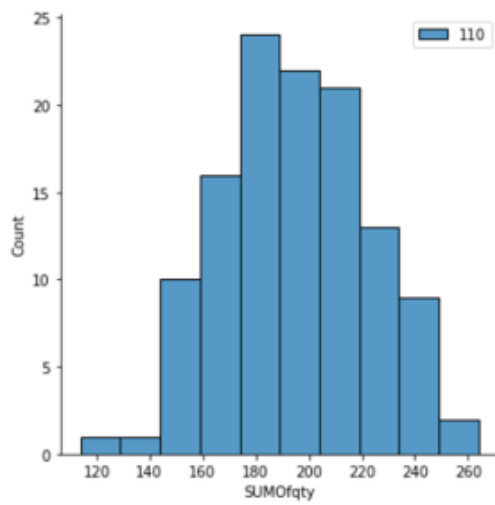
III. METHODOLOGY

➤ An iterative process that is applied across both product tiers



III. METHODOLOGY

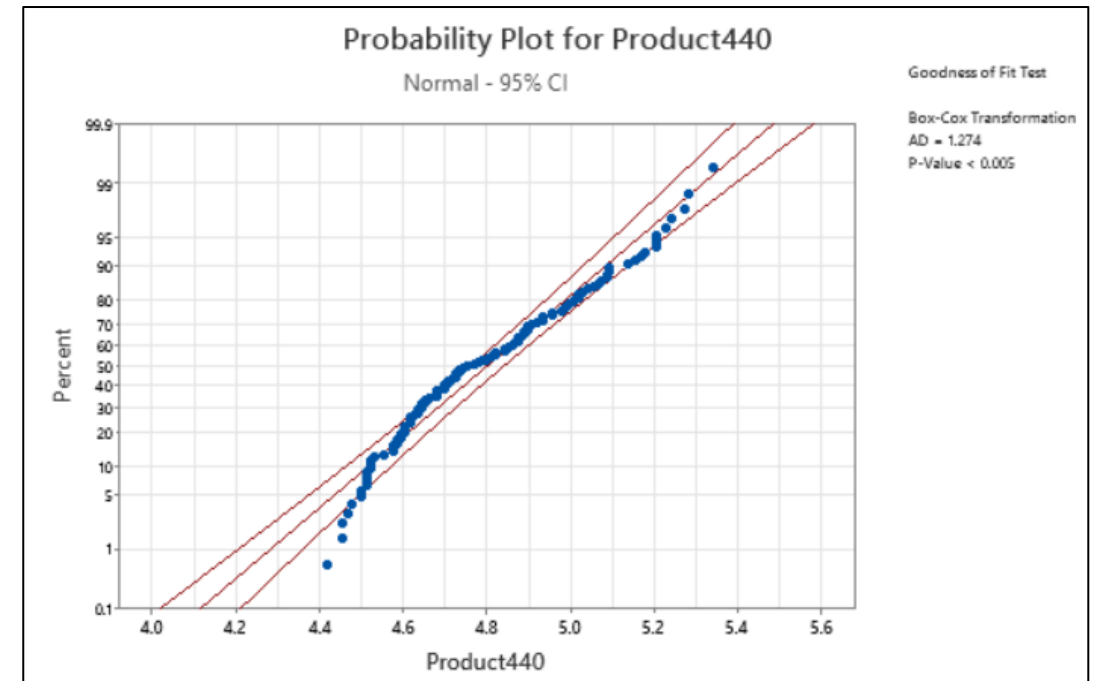
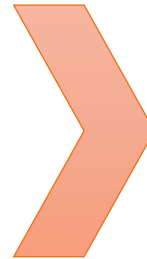
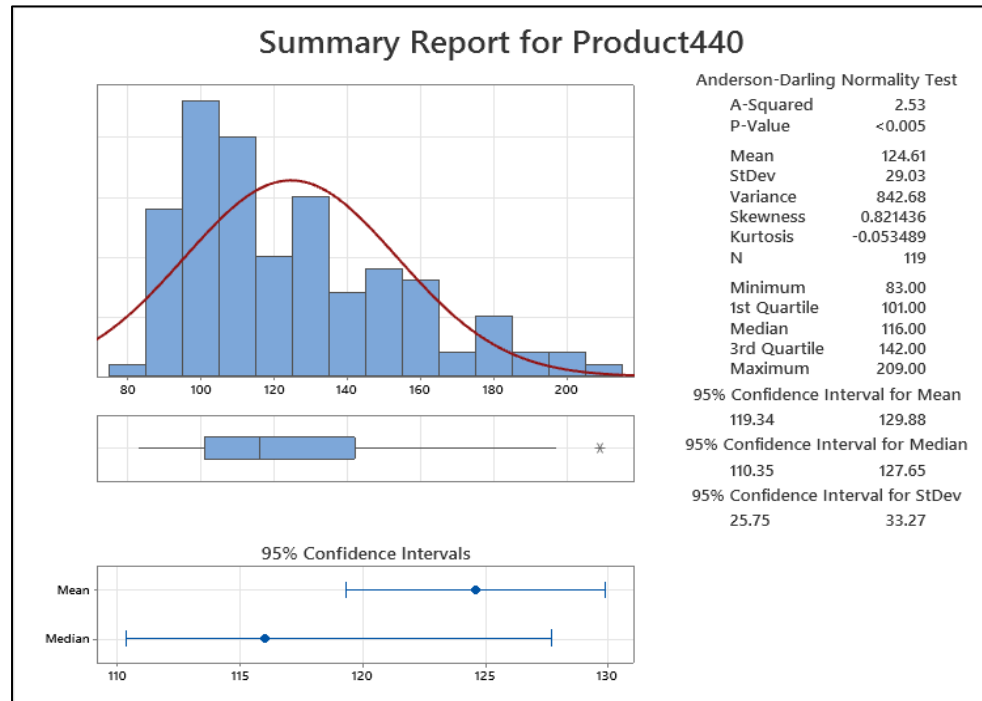
➤ Step 1: Graph distribution and gather descriptive statistics



- Majority of our products have their sale quantities that follow normal distributions
- Calculative the average and standard deviation for each product's sales based on normal distribution

III. METHODOLOGY

➤ Step 1: Graph distribution and gather descriptive statistics



- Some of our products whose sale quantities do not follow normal distributions
- Use Box-Cox to transform the data to normal distribution
- Calculate the average and standard deviation of the transformed distribution

III. METHODOLOGY

➤ Step 2: Estimate unit fixed cost

Rationale:

- Products with similar inventory value will have similar fixed cost

Clustering:

- Rank inventory value in ascending order
- Divide all records into 4 groups based on inventory value

Group Membership

- At member level, compute the average unit fixed cost, where:

$$\text{Unit Fixed Cost} = \frac{MOQ^2 * \text{Unit Holding Cost}}{2 * \text{Daily Sales Quantity}}$$

- Apply average unit fixed cost across all group members as followed:

| Group | Imputed Fixed Cost |
|-------|--------------------|
| 1 | \$ 47,160 |
| 2 | \$ 74,998 |
| 3 | \$ 81,197 |
| 4 | \$ 129,597 |

III. METHODOLOGY

➤ Step 3: Safety Stock and Inventory Calculations

❑ Continuous Review (R,Q) Policy


- $Demand_{LT} = \text{Average Daily Demand} * \text{Lead Time}$
- $Variance_{LT} = (\text{Std.Deviation from Daily Demand})^2 * \text{Lead Time}$
- $Standard\ Deviation_{LT} = \sqrt{Variance_{LT}}$
- $Z_{score} \text{ of } 99\% \text{ service level} = 2.3264$
- $Unit\ Holding\ Cost = \text{Inventory Value} * 10\%$
- $Safety\ Stock = Z_{score} * Standard\ Deviation_{LT}$
- $Reorder\ Point\ (R) = Demand_{LT} + Safety\ Stock$
- $EOQ\ (Q) = \sqrt{2 * \frac{Demand_{LT} * Unit\ Fixed\ Cost}{Unit\ Holding\ Cost}}$
- $Final\ Q = \text{Max}\ (EOQ\ \text{and}\ MOQ)$
- $On\text{-}hand\ Inventory = \left(\frac{Final\ Q}{2}\right) + safety\ stock$

❑ Periodic Review (T,S) Policy

- $Z_{score} \text{ of } 99\% \text{ service level} = 2.3264$
- $Safety\ stock = z_{score} * std.\ dev * \sqrt{(\text{Lead Time} + \text{Reorder Period})}$
- $Base\ Stock = \text{Daily Demand} * (\text{Lead Time} + \text{Reorder Period}) + safety\ stock$
- $On\text{-}hand\ Inventory = \frac{\text{Daily Demand} * \text{Reorder Period}}{2} + safety\ stock$

IV. FINDINGS

Product Tier 1 with 85 SKUs

| |  Continuous Review - (R,Q) Policy | Period Review - (T,S) Policy |
|--|--|------------------------------|
| \$ Total Inventory Cost | \$5,361,874 | \$5,361,874 |
| Avg. Inventory | 199,745 cases | 194,918 cases |
| Estimated T (Using Excel Goal Seek) | NA | 12.38 days |

- If it took the company less than 12.38 days to review inventory level, period review (T,S) policy would incur a lower inventory cost compared to continuous review (R,Q) policy
- Despite the cost saving, due to the nature of the tier 1 (high-priority products), it is recommended that the company continues using continuous review (R,Q) policy for this tier.

See Appendix – Slide #24 for Excel Goal Seek Analysis

IV. FINDINGS

Product Tier 2 with 68 SKUs

| | Continuous Review - (R,Q) Policy | ✓ Period Review - (T,S) Policy |
|--|----------------------------------|--------------------------------|
| \$ Total Inventory Cost | \$ 4164.87 | \$4131.71 |
| Avg. Inventory | 243 cases | 243 cases |
| Safety Stock | 3 cases | 10 cases |
| Estimated T (Using Excel Goal Seek) | NA | 117 days |

- If it took the company less than 117 days to review inventory level, period review (T,S) policy would incur a lower inventory cost compared to continuous review (R,Q) policy
- With similar average inventory and cost, it is recommended that the company continues using continuous review (R,Q) policy for this tier to maintain a low safety stock if T is greater than mentioned.

V. RECOMMENDATIONS



Products in Tier 1

- Keep applying continuous review - (R,Q) policy
- Avg. Inventory Cost = \$5.3 million
- Avg. On-hand Inventory = 199,745 cases
- Safety stock is recommended for each SKU



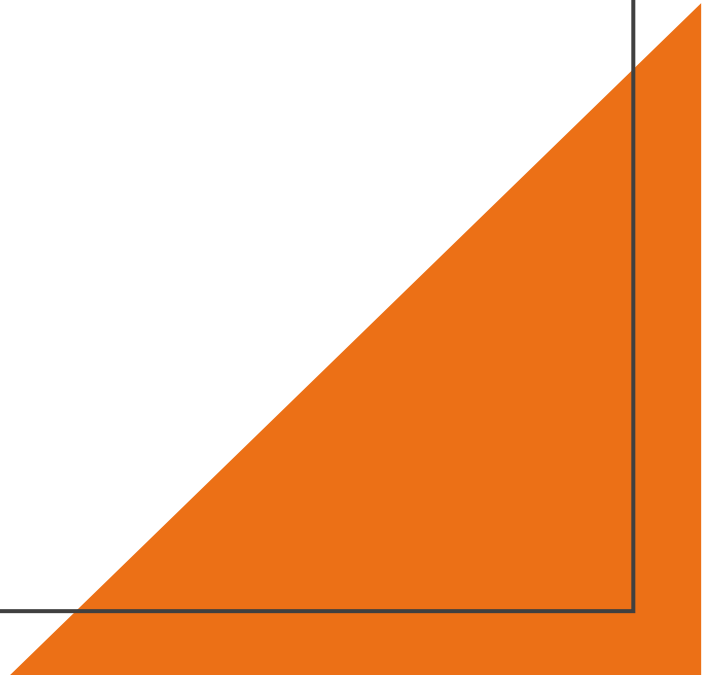
Products in Tier 2

- Apply periodic review - (T,S) policy if it takes less than 117 days to review
- Avg. Inventory Cost = \$4K
- Avg. On-hand Inventory = 243 cases
- Safety stock is recommended for each SKU

VI. LIMITATIONS/IMPLEMENTATION ISSUES

- Lack of information on nature of products and their categories could have impacted the final recommendations
- Sample size might not be representative of the entire inventory population
- Potential variances in the computed fixed costs could have skewed the results
- Organizational and logistic difficulty in implementing 2 policies based on the products

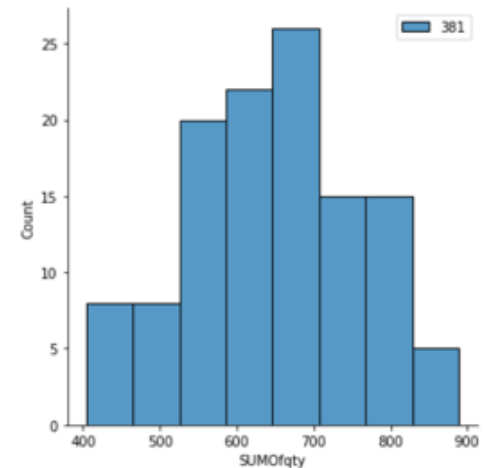
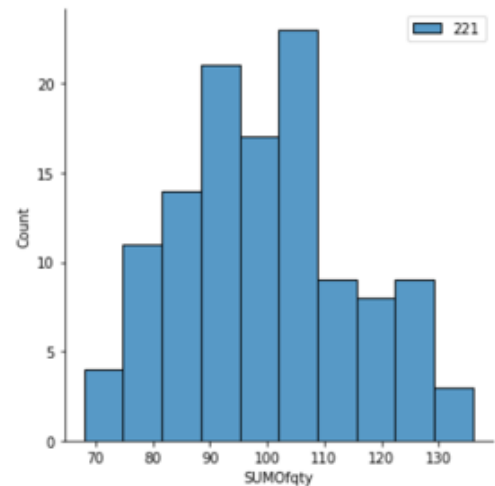
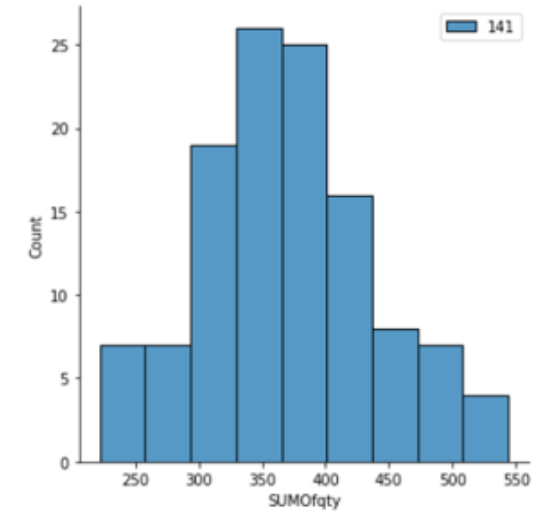
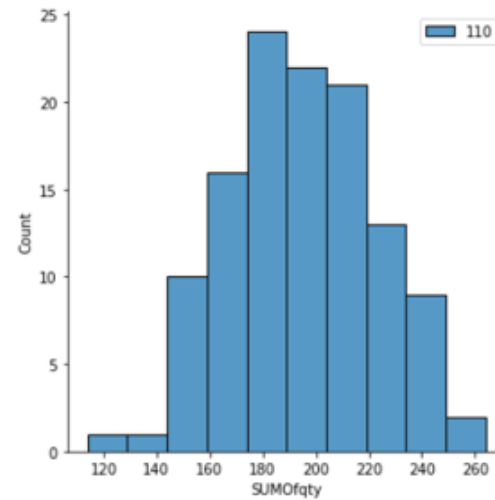
**THANK YOU FOR LISTENING
ANY QUESTIONS?**



APPENDIX

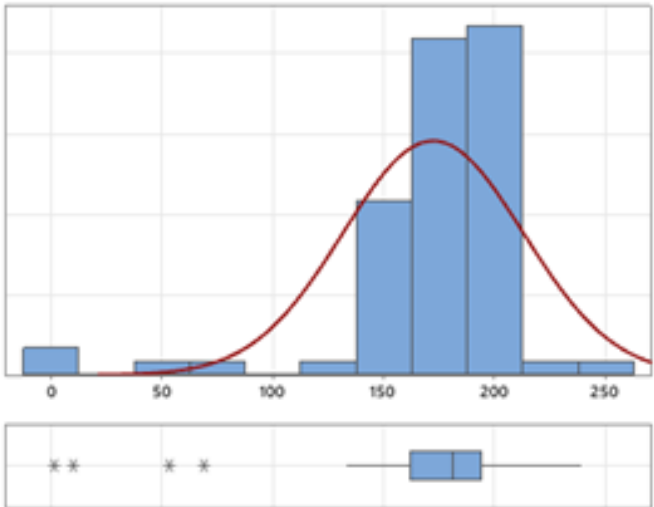
Graph Distribution of Daily Demand Across All SKUs

```
for product, data in df.groupby('product'):  
    sns.displot(data = data, x= data['SUMOfqty'], ax=ax, label=product)  
    plt.legend()  
    plt.show()
```



Example of Non-Normal Distribution of Daily Demand

Summary Report for Product447



Anderson-Darling Normality Test

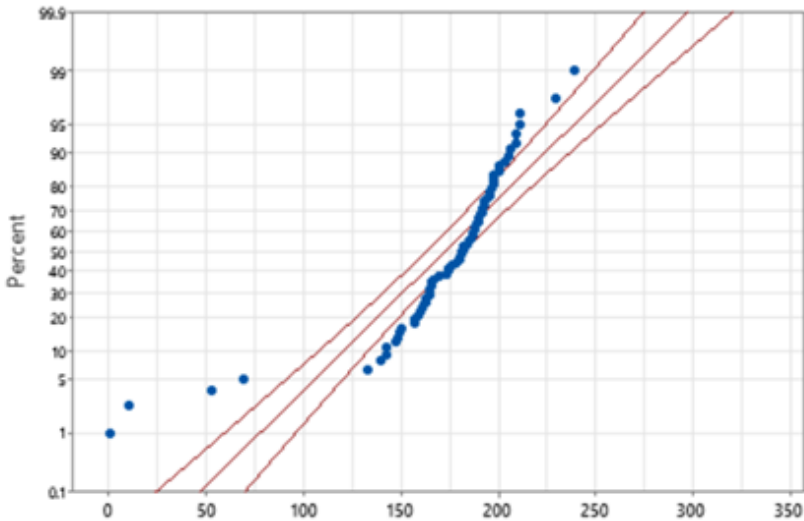
| | |
|--------------|----------|
| A-Squared | 4.65 |
| P-Value | <0.005 |
| Mean | 172.21 |
| StDev | 40.65 |
| Variance | 1652.43 |
| Skewness | -2.46552 |
| Kurtosis | 7.81416 |
| N | 71 |
| Minimum | 1.00 |
| 1st Quartile | 162.00 |
| Median | 181.00 |
| 3rd Quartile | 194.00 |
| Maximum | 239.00 |

| | | |
|------------------------------------|--------|--------|
| 95% Confidence Interval for Mean | 162.59 | 181.83 |
| 95% Confidence Interval for Median | 172.37 | 188.00 |
| 95% Confidence Interval for StDev | 34.89 | 48.71 |



Probability Plot for Product447

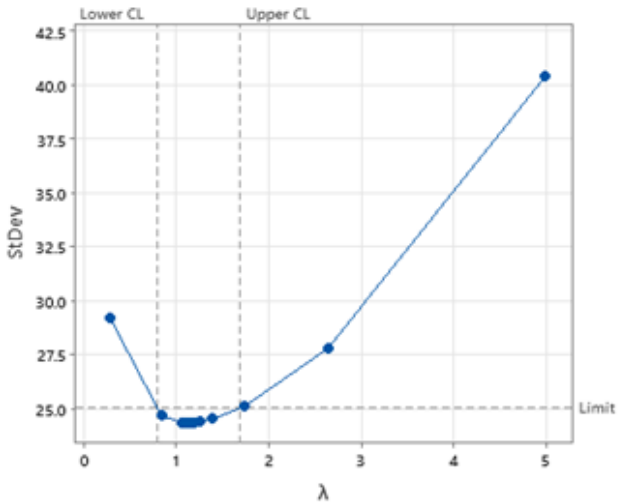
Normal - 95% CI



Goodness of Fit Test

Box-Cox Transform:
AD = 4.646
P-Value < 0.005

Box-Cox Plot of Product447

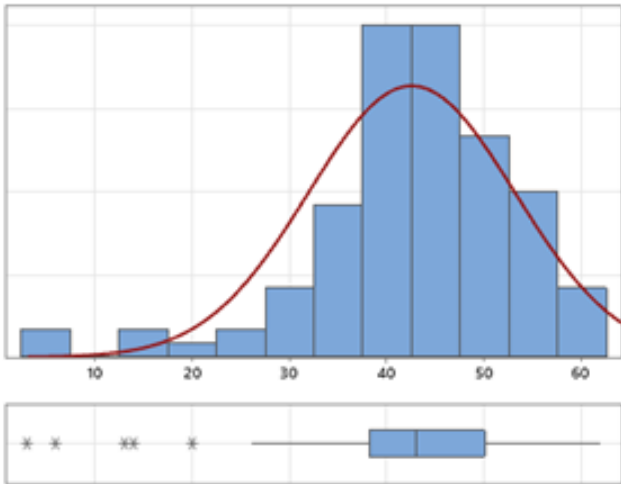


λ
(using 95.0% confidence)
Estimate 1.13
Lower CL 0.79
Upper CL 1.69
Rounded Value 1.00

Use Minitab to graph distribution and perform box-cox transformation with the optimal lambda value.

Example of Non-Normal Distribution of Daily Demand

Summary Report for Product640

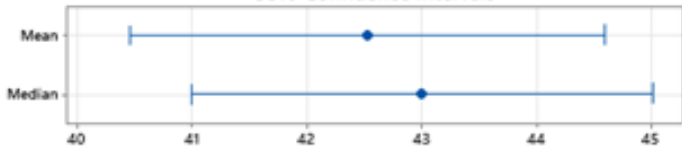


Anderson-Darling Normality Test

| | |
|--------------|----------|
| A-Squared | 1.62 |
| P-Value | <0.005 |
| Mean | 42.529 |
| StDev | 10.588 |
| Variance | 112.096 |
| Skewness | -1.14965 |
| Kurtosis | 2.68549 |
| N | 104 |
| Minimum | 3.000 |
| 1st Quartile | 38.250 |
| Median | 43.000 |
| 3rd Quartile | 50.000 |
| Maximum | 62.000 |

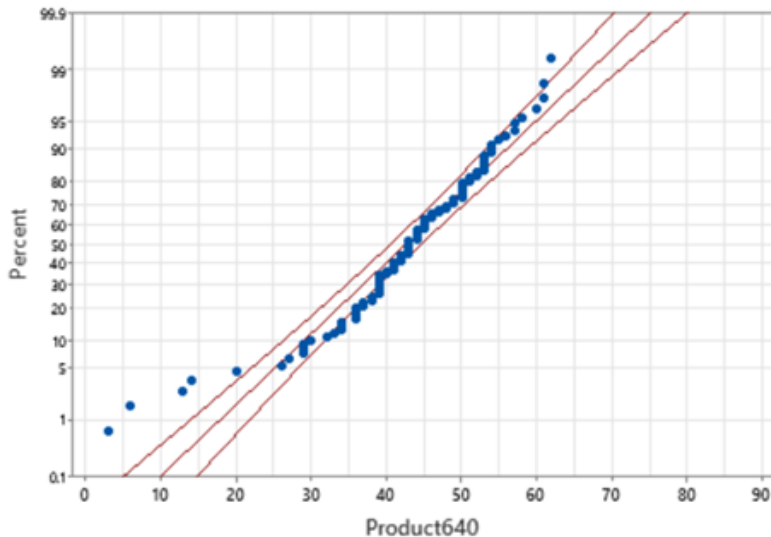
| | | |
|------------------------------------|--------|--------|
| 95% Confidence Interval for Mean | 40.470 | 44.588 |
| 95% Confidence Interval for Median | 41.000 | 45.000 |
| 95% Confidence Interval for StDev | 9.318 | 12.261 |

95% Confidence Intervals



Probability Plot for Product640

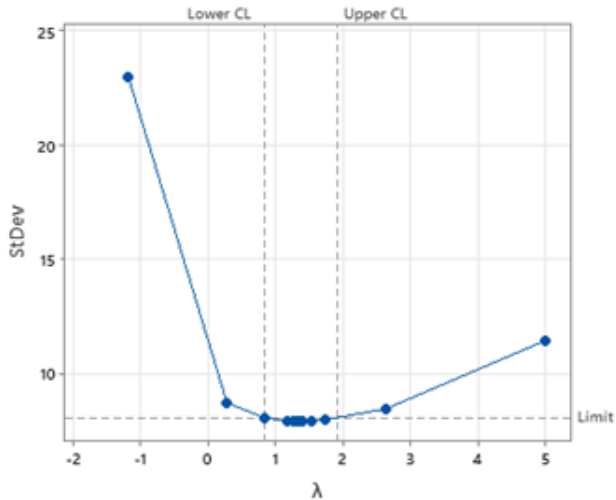
Normal - 95% CI



Goodness of Fit Test

Box-Cox Transformation
AD = 1.619
P-Value < 0.005

Box-Cox Plot of Product640

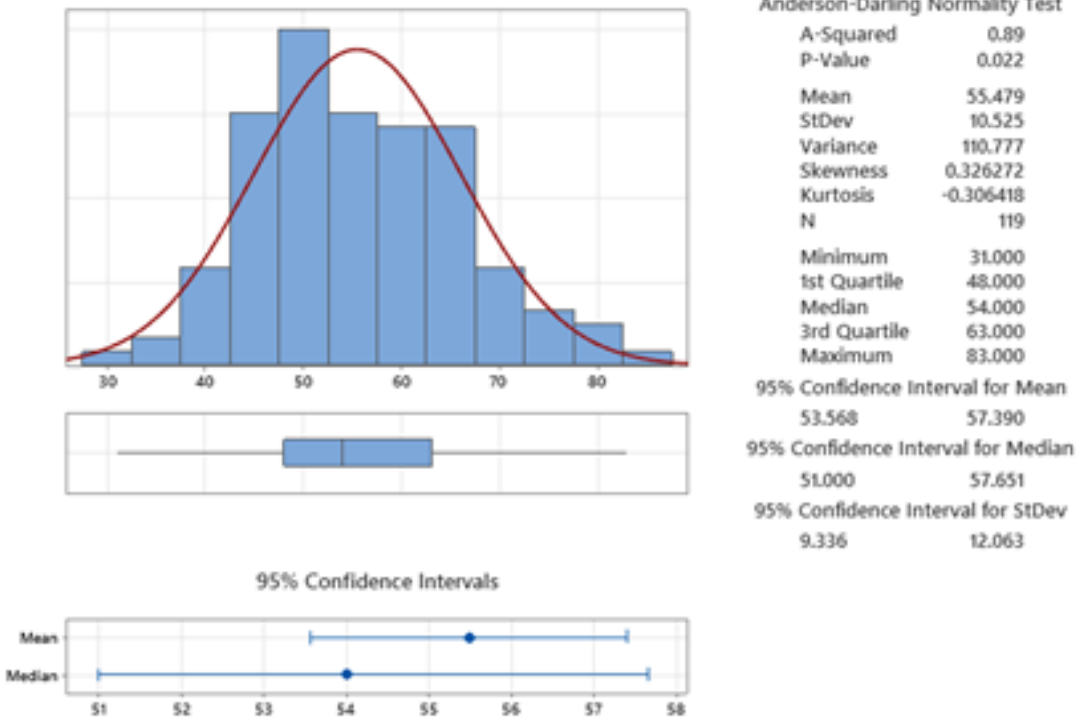


λ
(using 95.0% confidence)
Estimate 1.35
Lower CL 0.83
Upper CL 1.91
Rounded Value 1.00

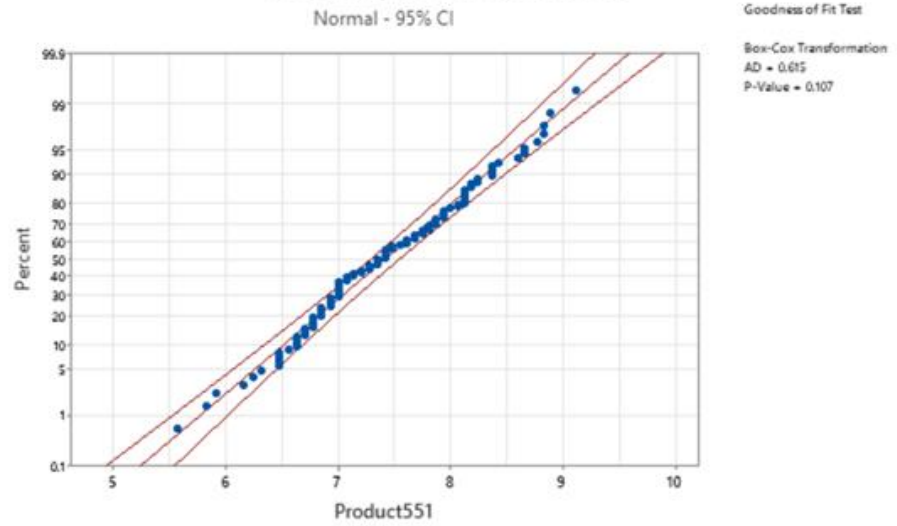
Use Minitab to graph distribution and perform box-cox transformation with the optimal lambda value.

Example of Non-Normal Distribution of Daily Demand

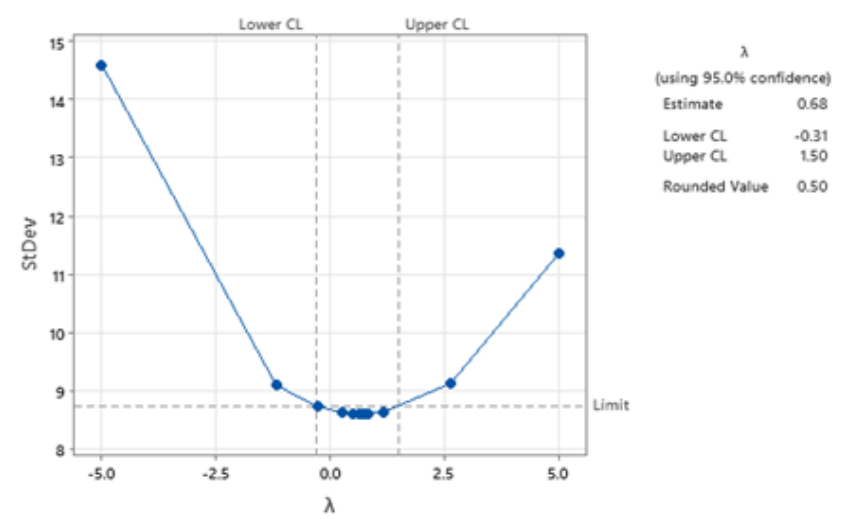
Summary Report for Product551



Probability Plot for Product551



Box-Cox Plot of Product551



Use Minitab to graph distribution and perform box-cox transformation with the optimal lambda value.

Descriptive Statistics Across All 680 SKUs (Mean, Standard Deviation)

```
In [7]: # Descriptive Statistics of daily demand (based on Total Quantity)
df1 = df.groupby("product")["SUMOfqty"].describe().reset_index()
df1
#df1.to_excel("output.xlsx")
```

Out[7]:


| | product | count | mean | std | min | 25% | 50% | 75% | max |
|-----|---------|-------|------------|-----------|-------|--------|-------|--------|-------|
| 0 | 100 | 36.0 | 1.166667 | 0.377964 | 1.0 | 1.00 | 1.0 | 1.00 | 2.0 |
| 1 | 101 | 119.0 | 112.159664 | 14.773994 | 81.0 | 102.00 | 110.0 | 119.50 | 160.0 |
| 2 | 102 | 41.0 | 36.585366 | 22.164133 | 1.0 | 11.00 | 46.0 | 52.00 | 67.0 |
| 3 | 103 | 51.0 | 1.450980 | 0.923336 | 1.0 | 1.00 | 1.0 | 2.00 | 6.0 |
| 4 | 104 | 3.0 | 1.000000 | 0.000000 | 1.0 | 1.00 | 1.0 | 1.00 | 1.0 |
| ... | ... | ... | ... | ... | ... | ... | ... | ... | ... |
| 674 | 774 | 1.0 | 1.000000 | NaN | 1.0 | 1.00 | 1.0 | 1.00 | 1.0 |
| 675 | 775 | 10.0 | 44.600000 | 58.939140 | 1.0 | 1.50 | 7.0 | 90.25 | 143.0 |
| 676 | 776 | 119.0 | 257.050420 | 33.778152 | 165.0 | 241.00 | 256.0 | 278.50 | 340.0 |
| 677 | 777 | 8.0 | 104.750000 | 69.236138 | 5.0 | 53.75 | 129.5 | 147.25 | 192.0 |
| 678 | 778 | 21.0 | 29.619048 | 31.265758 | 1.0 | 5.00 | 12.0 | 57.00 | 97.0 |

679 rows × 9 columns


Goal Seek Analysis To Find "T" for Tier 1 Under (T,S) Policy

| AI | AJ | AK | AL | AM | AN | AO |
|-------------------|------------------|---------------|----------------------|----|--------------------|--------------|
| Safety stock (TS) | Cycle stock (TS) | Inventory(TS) | Inventory Value (TS) | | T | 12.38 |
| 64.79613503 | 694.04445 | 758.840585 | \$ 16,307.48 | | Total \$ Inventory | \$ 5,361,874 |
| 124.2388357 | 1204.476781 | 1328.715617 | \$ 33,018.58 | | | |
| 102.9234824 | 1058.148686 | 1161.072168 | \$ 15,883.47 | | | |
| 2224.849066 | 21843.55016 | 24068.39923 | \$ 449,838.38 | | | |
| 122.4126727 | 1076.712698 | 1199.125371 | \$ 39,151.44 | | | |
| 270.4745816 | 2187.121418 | 2457.596 | \$ 29,982.67 | | | |
| 262.1961184 | 2299.545491 | 2561.741609 | \$ 18,598.24 | | | |
| 44.94870467 | 505.2323276 | 550.1810322 | \$ 33,082.39 | | | |
| 91.22706927 | 700.8044544 | 792.0315236 | \$ 29,542.78 | | | |
| 87.89043103 | 609.8563954 | 697.7468264 | \$ 49,819.12 | | | |
| 83.7137004 | 973.3366311 | 1057.050331 | \$ 19,830.26 | | | |
| 99.25703089 | 474.285865 | 573.5428959 | \$ 34,452.72 | | | |
| 60.57742907 | 354.9522301 | 415.5296592 | \$ 14,688.97 | | | |
| 46.90564263 | 370.3962401 | 417.3018828 | \$ 15,757.32 | | | |
| 65.4233321 | 615.2123989 | 680.635731 | \$ 14,191.25 | | | |

Goal Seek ? X

Set cell: 

To value:

By changing cell: 

Results for Tier 1 – 85 SKUs Under (R,Q) Policy

| SKU | Reoder Point | Quantity | Safety Stock | | | | | |
|-----|--------------|--------------|--------------|--------------|----------|--------------|----------|--------------|
| 101 | SKU | Reoder Point | Quantity | Safety Stock | | | | |
| 110 | 277 | 5,030 | SKU | Reoder Point | Quantity | Safety Stock | | |
| 114 | 283 | 2,554 | 277 | 5,030 | SKU | Reoder Point | Quantity | Safety Stock |
| 129 | 284 | 1,006 | 283 | 2,554 | 277 | 5,030 | 9,934 | 616 |
| 134 | 294 | 352 | 284 | 1,006 | 283 | 2,554 | 5,298 | 314 |
| 139 | 296 | 269 | 414 | 1,747 | 284 | 1,006 | 2,516 | 160 |
| 141 | 313 | 2,303 | 431 | 13,752 | 569 | 12,161 | 6,700 | 462 |
| 162 | 317 | 2,829 | 440 | 45 | 576 | 3,135 | 4,601 | 309 |
| 181 | 337 | 4,583 | 447 | 2,172 | 583 | 9,222 | 18,662 | 256 |
| 189 | 338 | 456 | 467 | 1,040 | 585 | 861 | 1,212 | 67 |
| 200 | 348 | 730 | 482 | 743 | 589 | 875 | 1,787 | 2,603 |
| 201 | 355 | 574 | 486 | 589 | 593 | 8,214 | 7,702 | 3,211 |
| 205 | 376 | 694 | 488 | 2,271 | 598 | 6,692 | 10,312 | 3,955 |
| 217 | 378 | 2,138 | 490 | 3,078 | 605 | 1,644 | 3,710 | 795 |
| 221 | 381 | 4,680 | 491 | 1,092 | 609 | 1,550 | 3,711 | 1,602 |
| 225 | 383 | 2,467 | 508 | 1,913 | 624 | 453 | 1,724 | 397 |
| 263 | 397 | 2,859 | 514 | 769 | 626 | 3,840 | 5,731 | 1,619 |
| 265 | 402 | 5,984 | 519 | 453 | 636 | 10,312 | 5,736 | 977 |
| | 403 | 8,879 | 528 | 1,960 | 640 | 120 | 736 | 1,960 |
| | 410 | 1,992 | 538 | 1,150 | 645 | 2,394 | 4,763 | 695 |
| | | | 540 | 1,179 | 649 | 394 | 765 | 3,278 |
| | | | 551 | 97 | 652 | 28,662 | 25,776 | 2,346 |
| | | | 567 | 1,919 | 666 | 303 | 1,666 | 45 |
| | | | | | 668 | 922 | 1,565 | 101 |